

## The Proof of Ernest Ferron's formula to find the slope of a saxophone neck in "The Saxophone is my Voice"

Important: The measurement of the slope of a cone is its "half angle".

The formula for slope as a **ratio** or "proportion" is  $\text{slope} = \text{rise}/\text{run}$ .

The rise is the large radius  $R$  minus the small radius  $r$ .

In the case of a complete cone, the small radius  $r$  is always equal to 0.

The "run" or height (or length) of the cone is represented by  $h$  or  $L$ .

Representing the slope in a circle,  $h$  or  $L$  or the "run" is equal to the radius.

The distance traveled along the arc of the circle equal to the length of the radius is called a **radian**. Since  $C = \pi D$ ,  $C = \pi 2r$  is also true.

$2\pi r =$  the circumference of a circle or  $360^\circ$

$\pi r =$  half the circumference or  $180^\circ$

Since  $r$  (or  $h$ ) = 1 radian, 1 radian =  $180^\circ/\pi$  or  $57.3^\circ$

Inputting the figures derived from calculating the length of the missing cone by frequency, we get the following equation:

slope as a proportion =  $R - r \div L$  Where  $R = 6.3\text{mm}$ ,  $r = 0$ ,  $L = 225.3\text{mm}$

slope as a proportion =  $(6.3\text{mm} - 0)/225.3 = .028$

We know by this formula that the rise is .028 of the length.

We also know that the length ( $L$ ) is equal to the radius of the circle ( $R$ )

Also by definition: the radius and radian are equal length.

1 radian =  $57.3^\circ$ , so the proportion of the rise in degrees is  $57.3^\circ \times .028$

Therefore the slope in degrees is  $57.3^\circ \times .028 = 1.60^\circ$

Where Ferron confuses the issue is that instead of:

slope in degrees =  $57.3 (R - r)/L$

he uses

$28.65 (D - d)/L$  which gives the same result!

